

ON THE UNIFORM CONVERGENCE OF THE GENERALIZED BIEBERBACH POLYNOMIALS IN REGIONS WITH K -QUASICONFORMAL BOUNDARY

Abstract

Let G be a finite domain in the complex plane with K -quasiconformal boundary, z_0 be an arbitrary fixed point in G and $p > 0$. Let $\varphi(z)$ be the conformal mapping from G onto the disk with radius $r_0 > 0$ and centered at the origin 0, normalized by $\varphi(z_0) = 0$ and $\varphi'(z_0) = 1$. Let us set $\varphi_p(z) := \int_{z_0}^z [\varphi'(\zeta)]^{1/p} d\zeta$, and let $\pi_{n,p}(z)$ be the generalized Bieberbach polynomial of degree n for the pair (G, z_0) that minimizes the integral $\iint_G |\varphi'_p(z) - P'_n(z)|^p d\sigma_z$ in the class \tilde{A}_n of all polynomials of degree $\leq n$ and satisfying the conditions $P_n(z_0) = 0$ and $P'_n(z_0) = 1$. In this work we prove the uniform convergence of the generalized Bieberbach polynomials $\pi_{n,p}(z)$ to $\varphi_p(z)$ on \bar{G} in case of $p > 2 - \frac{K^2 + 1}{2K^4}$.