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ON FATIGUE WEAR EQUATION WITH REGARD TO THERMAL EFFECTS

Abstract

*The fatigue wear equation with regard to thermal effects that admits define the time and number of cycles of the fatigue wear of materials is constructed.*

As is known, there exist some classifications of wear forms [1]. Fatigue wear occupies a special place among them [2]. It is stipulated by multiple repeated deformation of surface layers that reduce to formation of damages, and as a final result to the disturbance of strength (continuity) of surface layers. Therefore the investigation of fatigue wear process of surface layers from the point of view of accumulation of damages [3-7] has a real meaning. In this direction a good attempt was made in paper [8], where on the basis of the conception of Kachanov-Rabotnov damages the fatigue wear equation is obtained. And here residual deformation in a surface layer is chosen as a fatigue wear factor. However, as known, temperature of surface layer plays an essential role at fatigue wear that is not taken into account in [8]. We make up a deficiency in some degree.

Following [5-7] we introduce some scalar  $0 \leq \Pi \leq 1$ . The quantity  $\Pi$  characterizes the damageability of the surface layer of material; it increases depending on the time  $t$  or the number of cycles  $N$  from 0 to 1. Here  $\Pi(0) = 0$ ,  $\Pi(t_c) = 1$  or  $\Pi(N_c) = 1$ , where  $t_c$  is time,  $N_c$  is the number of cycles under which the fatigue wear of material occurs. If we denote the beginning of the  $k$ -th cycle by  $t_k$  ( $t_0 = 0$ ) the duration of the  $k$ -th cycle will be  $t_k - t_{k-1}$  ( $k = 1, 2, \dots, N_c$ ). In addition  $t_c = \sum_{k=1}^{N_c} (t_k - t_{k-1})$ . If we adopt the duration of each cycle equal  $t$ , among themselves, we have  $N = t/t_c$ ,  $N_c = t_c/t$ . The residual intensity of deformations  $\varepsilon_{+p}^0$  for each embedding cycle we take as a defining parameter effecting on the fatigue wear process as in [8]. The temperature  $T(x, t)$  where  $(x) = (x_1, x_2, x_3)$ ,  $t \in [0, t_c]$  we adopt as the other defining parameter. We adopt that the quantities  $\varepsilon_{+p}^0(x, t)$  and  $T(x, t)$  are known from the solution of corresponding problems. In further records we omit the arguments  $x$ .

We adopt the alternation of accumulated damages in the form

$$\frac{d\Pi}{dt} = f(\Pi)\varphi_1(\varepsilon_{+p}^0, T). \tag{1}$$

In (1) it is admitted an independent effect of the quantities  $\frac{d\Pi}{dt}$  and  $\Pi$  on  $\varphi_1(\varepsilon_{+p}^0, T)$ .

As a result of integration of the equation (1) provided  $\Pi(t_c) = 1$  we get

$$\int_0^{t_c} \varphi_1(\varepsilon_{+p}^0(t), T(t)) dt = 1, \tag{2}$$

where  $\varphi = \frac{\varphi_1}{A}$ ,  $A = \int_0^1 \frac{d\Pi}{f(\Pi)} = const$ .

We approximate the function  $\varphi(\varepsilon_{+p}^0, T)$  in the form of power functions

$$\varphi(\varepsilon_{+p}^0, T) = B(\varepsilon_{+p}^0)^\beta \left(\frac{T}{T_s}\right)^\delta, \quad (3)$$

where  $B, \beta, \delta$  are universal constants of material,  $T_s$  is some constant reduction temperature which is chosen from the alternation range of temperature  $T$ .

We adopt the relation (2) with regard to (3) in the form of

$$\int_0^{t_0} (\varepsilon_{+p}^0(t))^\beta \left(\frac{T(t)}{T_s}\right)^\delta dt = \frac{1}{B}. \quad (4)$$

Under arbitrary constants  $\varepsilon_{+p}^0 = \varepsilon_{+p}^{00} = \text{const}$ ,  $T = T_0 = \text{const}$  it follows from (4) that

$$(\varepsilon_{+p}^{00})^\beta \left(\frac{T_0}{T_s}\right)^\delta t_0 = \frac{1}{B}, \quad (5)$$

where  $t_0$  is fatigue wear time under the constants  $\varepsilon_{+p}^{00}$  and  $T_0$ .

We use the results of experiments of the fatigue wear with equal duration  $t_*$  of each cycle. Let  $\varepsilon_c$  and  $T_c$  be critical intensities of deformation and temperature after single imbedding for time  $t_*$ . Moreover it follows from the equation (4) that

$$\varepsilon_c^\beta \left(\frac{T_c}{T_s}\right)^\delta t_* = \frac{1}{B}. \quad (6)$$

Comparing the relations (5) and (6) we get

$$\frac{t_0}{t_*} (\varepsilon_{+p}^{00})^\beta = \varepsilon_c^\beta \left(\frac{T_c}{T_0}\right)^\delta$$

or

$$N_0^{\frac{1}{\beta}} \varepsilon_{+p}^{00} = \varepsilon_c \left(\frac{T_c}{T_0}\right)^{\frac{\delta}{\beta}}, \quad (7)$$

where  $N_0 = \frac{t_0}{t_*}$  is the number of cycles before the fatigue wear begins for

$\varepsilon_{+p}^0 = \varepsilon_{+p}^{00} = \text{const}$  and  $T = T_0 = \text{const}$ .

In references there are tests represented by the relations [9-11]

$$N_0^\alpha \varepsilon_{+p}^{00} = C. \quad (8)$$

And they note that one can consider the quantity  $\alpha$  not depending on temperature, and the quantity  $C$  is, generally speaking, a difference function of temperatures  $\Delta T_0 = \text{const}$ , i.e.  $C = C(\Delta T)$ . For example, in [11] the equation of fatigue wear is obtained experimentally for the alloy of the mark 45  $\varepsilon_{+p}^{00} N_0^{0.4} = 0.06$ .

The quantity  $C$  which is contained in relation (8) in references in majority of cases is represented as

$$C(T) = C_0 \left(\frac{T_s}{T}\right)^\gamma \quad (C_0, \gamma = \text{const}). \quad (9)$$

The comparison of relations (7) and (8) with regard to (9) gives the following results:

$$\frac{1}{\beta} = \alpha, \quad \varepsilon_c = C_0; \quad \left(\frac{T_c}{T_0}\right)^{\delta/\beta} = \left(\frac{T_s}{T}\right)^\gamma. \quad (10)$$

If for  $T_s$  we choose  $T_c$  and adopt  $T = T_0$ , we get from (10)  $\delta/\beta = \gamma$ . Hence  $\delta = \beta\gamma = \frac{\gamma}{\alpha}$ .

Consequently, the questions on the experimental definition of constants are settled. Since the obtained constants are considered to be universal constants of material, then equaling the relations (4) and (6) we get:

$$\int_0^{t_c} (\varepsilon_{+p}^0(t))^\beta \left( \frac{T(t)}{T_c} \right)^\delta dt = \varepsilon_c^\beta t_c. \quad (11)$$

The relation (11) is an equation of fatigue wear of the surface layers of material. It determines time  $t_c$  and the number of cycles  $N_c$  of the fatigue wear. Note that the relation (11) for  $t_k - t_{k-1} = t$ , for any  $k$ , for  $T(t) = T_c = \text{const}$  coincides with analogic equation obtained in [8].

Finally, note that the equation (11) may be used as a criterium for small cycle (mechanical) and thermal fatigue.

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